

THE MEASURING OF ASSORTATIVENESS IN MARRIAGE: A COMMENT

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The measuring of assortativeness in marriage: a comment*

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Abstract

Measuring the extent to which such assortative matching differs between two economies is challenging when the marginal distributions of the characteristic along which sorting takes place (e.g. education) also changes for either or both sexes. Drawing from the statistics literature we define simple conditions that any index has to satisfy to provide a measure of change in sorting that is not distorted by changes in the marginal distributions of the characteristic. While most indices used in the literature satisfy these conditions, one of them – the likelihood ratio of [Eika et al. \(2019\)](#) – does not. We attribute their empirical result of declining homogamy at the top of the distribution to the violation of our conditions.

1 Introduction

The study of sorting in the marriage market has recently attracted renewed attention. The degree of homogamy in marriage - defined as people's tendency to 'marry their own' - has important consequences for family inequalities and intergenerational transmission of human capital. It is therefore surprising that the various studies on this topic have not reached a

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consensus on the evolution of homogamy over the recent years, and even on how to best measure homogamy (e.g. [Chiappori et al., 2017](#); [Ciscato and Weber, 2020](#); [Eika et al., 2019](#); [Fernández and Rogerson, 2001](#); [Greenwood et al., 2014](#); [Mare and Schwartz, 2005](#); [Siow, 2015](#), to mention but a few).

The goal of this comment is to understand why different approaches to the same problem, using similar data, can reach opposite conclusions and, more generally, to clarify the theoretical issues underlying the choice of a particular measure of assortativeness.

Our analysis considers two populations, say women and men, sorting in marriage according to a one-dimensional characteristic, say education. Whenever the marginal distributions change – e.g., women’s average education increases – matching patterns will change. The main problem faced by any measure of assortativeness is to disentangle the mechanical effects of such variations in the marginal distributions from deeper changes in the matching structure itself, for instance originating from changes in the gain generated by assortativeness along that characteristic. The latter represents what one would call ‘changes in homogamy’. Existing studies proposed various indices to measure assortativeness and changes therein. These indices achieve this goal in different ways, and may therefore generate diverging conclusions. Here we argue that *(i)* all acceptable indices should satisfy some basic requirements that we describe below; *(ii)* empirically, the most commonly used indices satisfying these requirements all conclude that educational homogamy has increased in the US at the top of the distribution over the last two decades, while on the contrary the index in [Eika et al. \(2019\)](#), which violates several conditions, leads to the opposite conclusion; and *(iii)* in general, it is useful that the index be based on a well specified structural model, so that the way it operates can be clearly understood.

2 Measuring assortative matching and changes in assortativeness

We first define assortativeness and changes therein in a 2×2 matching market, where each participant on either side of the market is in one of two groups defined by some characteristic such as education. Later in this Section we will argue that assortativeness is fundamentally a local concept and, hence, global measures aiming to summarise it over a wider range of values for the characteristic of interest fail to detect variation in different margins and are difficult to interpret. For simplicity, we will discuss positive assortativeness and increases in positive assortativeness, but a symmetric discussion could be held for negative assortativeness.

2.1 Defining Assortative Matching

We start with a simple example. Consider an economy where an equal mass of men and women match by their level of education, which can only take two values - say, High School versus College. We will abstract from singles - everybody gets matched. The matching patterns in this population are summarized by the 2×2 matching Table (a, b, c, d) shown below. In the Table, $a + b$ and $a + c$ are the number of female and male college graduates respectively, while a is the number of couples where both spouses are college graduates. In what follows, we assume that $b \geq c$, i.e. that women are more educated than men; the alternative case obtains by switching b and c .

Table (a, b, c, d)

$w \setminus h$	C	HS
C	a	b
HS	c	d

We say that Table (a, b, c, d) exhibits Positive Assortative Matching (PAM) if *the num-*

ber of couples with equal education (the ‘diagonal’ of the Table) is larger than what would obtain under random matching. Under random matching the number of couples where both spouses are college graduates will simply be $\frac{(a+b)(a+c)}{a+b+c+d}$. Then we have PAM if and only if $a(a+b+c+d) \geq (a+b)(a+c)$ or equivalently if $ad \geq bc$; this also implies that more High School graduates marry each other than would be implied by random matching: $d(a+b+c+d) \geq (b+d)(c+d)$.

2.2 Defining ‘increases in Assortative Matching’: required properties

We now consider two Tables, $T = (a, b, c, d)$ and $T' = (a', b', c', d')$, and ask under what conditions can it be concluded that T is more assortative than T' . In other words, how can we define an Assortativeness Index $I(a, b, c, d)$ that quantifies the ‘degree of assortativeness’ of a Table? We define four basic properties that all indices of assortativeness should satisfy.

Scale Invariance Any index I should not depend on the total size of the population, i.e.:

$$I(\lambda a, \lambda b, \lambda c, \lambda d) = I(a, b, c, d) \text{ for all } \lambda > 0.$$

Symmetry Any index I should treat the two categories (here, C and HS) identically; in other words, the index characterizes the level of assortativeness of the whole table. In practice, thus: $I(a, b, c, d) = I(d, c, b, a)$.

Monotonicity Consider the case where the two tables T and T' represent the same total population ($a + b + c + d = a' + b' + c' + d'$) with *identical marginal distributions* - i.e., the same proportion of educated men and women so that $a + b = a' + b'$ and $a + c = a' + c'$. In this case, Monotonicity requires that more assortativeness is equivalent to more people in each diagonal cell. So T is more assortative than T' if a larger fraction of individuals marry

their own type in Table T than in Table T' . Formally:

$$a \geq a' \quad \text{or equivalently} \quad d \geq d'.$$

Perfect PAM We introduce two forms of this condition, weak and strong. The strong form relates to the polar case that obtains when all educated men marry educated women. This implies $c = 0$ and the sorting Table is $T = (a, b, 0, d)$. T is *perfectly (positive) assortative* in the sense that all educated individuals in the less educated population (men in our example) marry a spouse in the same education group as themselves; the only ‘cross-marriages’ result from the fact that educated women are more numerous than educated men.

The strong version of Perfect PAM states that T displays maximum degree of assortativeness, so no other Table can display strictly more assortativeness than T . So if a ranking of Tables by assortativeness is defined by an index, this index should reach its maximum value for T .

A weaker version of the condition applies to populations with an equal proportion of educated men and women. In that case, Perfect PAM obtains when $c = 0$ and $b = 0$, so all educated individuals marry their own. In statistical terms, the association between spouses’ educations is then *absolute* in the sense of [Kendall and Stuart \(1961\)](#). Weak Perfect PAM therefore states that no Table can display strictly more assortativeness than Table $(a, 0, 0, d)$. Clearly, Perfect PAM implies the Weak version, while the converse is not true.

Our main claim is that *any acceptable measure of assortativeness must satisfy (at least) Scale Invariance, Symmetry, Monotonicity and Weak Perfect PAM*. In particular, it cannot be the case that a Table in which all individuals marry their own is found to be strictly less assortative than a Table that includes cross-marriages. As we shall see, imposing these conditions has bite, since some existing indices violate some of them.

2.3 Existing indices

We now briefly review some of the most commonly used indices in the literature.

Odds Ratio This is probably the most widely used index:

$$I_O(a, b, c, d) = \ln \left(\frac{ad}{bc} \right)$$

The odds ratio is popular in the demographic literature, as it can be directly derived from the log-linear approach (see for instance [Mare \(2001\)](#), [Mare and Schwartz \(2005\)](#), [Bouchet-Valat \(2014\)](#)); in economics, it was used by [Siow \(2015\)](#) ('local odds ratio') [Chiappori et al. \(2017\)](#), [Ciscato and Weber \(2020\)](#), [Chiappori, Costa-Dias, Crossman and Meghir \(2020\)](#) among many others.

Correlation A natural index is the correlation between wife's and husband's educations, each considered as a Bernoulli random variable taking the value C with probability $\frac{a+b}{a+b+c+d}$ (resp. $\frac{a+c}{a+b+c+d}$) and HS with probability $\frac{c+d}{a+b+c+d}$ (resp. $\frac{b+d}{a+b+c+d}$). This has been used in various contributions (for instance [Greenwood et al., 2003, 2014](#)), either explicitly or through a linear regression framework. Here:

$$I_{Corr}(a, b, c, d) = \frac{ad - bc}{\sqrt{(a+b)(c+d)(a+c)(b+d)}}$$

One can readily check that, in our case, the correlation index also coincides with Spearman's rank correlation, which exploits the natural ranking of education levels ($C > HS$). Equivalently, one can consider the χ^2 index, which is $\chi^2(a, b, c, d) = [I_{Corr}(a, b, c, d)]^2$

Minimum Distance In the minimum distance approach of [Fernández and Rogerson \(2001\)](#) and [Abbott et al. \(2019\)](#), one constructs the convex combination of two extreme cases (random and perfectly assortative) that minimizes the distance with the Table under

consideration, and defines the weight of the perfectly assortative component as the index. Here, it is equal to:

$$I_{MD}(a, b, c, d) = \frac{ad - bc}{A}$$

where $A = (c + d)(a + c)$ if $b \geq c$ and $A = (b + d)(a + b)$ if $c \geq b$. This coincides in our context, with the ‘perfect-random normalization’ of [Liu and Lu \(2006\)](#) and [Shen \(2019\)](#).

Likelihood Ratio [Eika et al. \(2019\)](#) measure marital sorting between men of education level I and women of education level J “as the observed probability that a husband with education level I is married to a wife with education level J , relative to the probability under random matching with respect to education”. In practice, this leads to a specific index, namely the likelihood ratio:

$$I_L(a, b, c, d) = \frac{a(a + b + c + d)}{(a + b)(a + c)}$$

2.4 Properties of the indices of assortativeness

2.4.1 The main result

The following summarises the properties of the indices of assortativeness defined above:

Result *Among indices just described:*

- *The odds ratio and the minimum distance index both satisfy Scale Invariance, Symmetry, Monotonicity and Perfect PAM (therefore Weak Perfect PAM).*
- *Correlation and Spearman rank correlation both satisfy Scale Invariance, Symmetry, Monotonicity and Weak Perfect PAM but not Perfect PAM.*
- *The Likelihood ratio satisfies Scale Invariance and Monotonicity; it does not satisfy Symmetry nor Weak Perfect PAM.*

We argue that the likelihood ratio is not an adequate measure because it violates two of the basic properties that an index of assortativeness should satisfy. It violates symmetry by singling out one category (here College); applied to the alternative category (High School), it would result in a different value for the index. It also violates Weak Perfect PAM as demonstrated by the following simple example. We compare Tables A and B corresponding, for instance, to two different cohorts in the same economy (population sizes normalized to 1):

Table $A = (.03, .07, .07, .83)$

$w \setminus h$	C	HS
C	.03	.07
HS	.07	.83

Table $B = (.5, 0, 0, .5)$

$w \setminus h$	C	HS
C	.5	0
HS	0	.5

The distribution of education is independent of gender in both A and B , but the number of educated people has increased from 10% to 50% between A and B . Cohort A exhibits PAM in the usual sense (more people on the diagonal than would obtain under random matching); yet, 70% of educated people marry an uneducated spouse. Cohort B displays perfect PAM, with all college educated individuals marrying together. Consistently, all indices discussed above satisfying Weak Perfect PAM conclude that B displays more assortativeness than A . However, the likelihood ratio yields $I_L(A) = 3$ and $I_L(B) = 2$, suggesting that assortativeness has *decreased* from A to B - a conclusion that is intuitively quite difficult to accept.

2.4.2 Marginal Independence

To explain this paradox, it is interesting to refer to an older statistical literature that discusses the properties of measures of association in the case of paired attributes (i.e., in our case, husband's and wife's education). The Marginal Independence requirement posed by [Edwards \(1963\)](#) states that the association should not be 'influenced by the relative sizes of the

marginal totals' (p. 110). That is, the measure should not change if one starts from a Table $T(a, b, c, d)$ and doubles the number of couples where the man is educated (while keeping unchanged the ratio of educated versus uneducated wives). Formally, for any non negative (a, b, c, d) and any positive λ , it should hold that:

$$I(\lambda a, \lambda b, c, d) = I(\lambda a, b, \lambda c, d) = I(a, \lambda b, c, \lambda d) = I(a, b, \lambda c, \lambda d) = I(a, b, c, d)$$

Edwards (1963) explains that the measure must only be a function of *the proportion of educated women whose husband is educated and the proportion of uneducated women whose husband is educated* (and conversely), so that any population change that keeps these proportions constant should not affect the index. The condition was later generalized by Altham (1970) to the $n \times n$ case.

Among the indices just reviewed, only one - the odds ratio - satisfies Edwards's marginal invariance. It is interesting to consider *how* the other indices violate this requirement. Consider Table $T_\lambda = (\lambda a, \lambda b, c, d)$ with $ad > bc$ and $\lambda \geq 1$. Suppose λ increases. Then:

- The minimum distance index *increases* since $\partial I_{MD}/\partial \lambda > 0$;
- The likelihood ratio *decreases* since $\partial I_{LR}/\partial \lambda < 0$;
- The correlation and Spearman correlation may increase or decrease depending on parameters.

In the previous example, educational attainment increases between cohorts A and B . This mechanically generates a reduction in the likelihood ratio, driving the paradoxical result.

2.5 Structural interpretations

Finally, it is important to note that among the various indices, the odds ratio has the additional advantage of having a known structural interpretation. Specifically, assume that the observed matching behavior constitutes the stable equilibrium of a frictionless matching

model under transferable utility. Assume, furthermore, that the surplus generated by a match between woman i belonging to category I and man j belonging to category J takes the separable form:

$$s(i, j) = Z^{IJ} + \alpha_i^J + \beta_j^I$$

where Z is a deterministic component depending only on individual educations and the α, β are random shocks reflecting unobserved heterogeneity among individuals. It is now well known (Graham (2011), Chiappori (2017)) that, keeping constant the distribution of the shocks, assortativeness is related to the supermodularity of the matrix Z^{IJ} (i.e., in the 2×2 case, to the sign of the supermodular core $Z^{HS,HS} + Z^{C,C} - Z^{HS,C} - Z^{C,HS}$). More importantly, if, following the seminal contribution by Choo and Siow (2006), one assumes that the random shocks follow Type 1 extreme value distributions (the so-called Separable Extreme Value or SEV model), then the supermodular core equals twice the odds ratio I_O .

This structural interpretation is especially useful for disentangling possible changes in the value of different matches from the mechanical effect of variations in the marginal distributions of education among individuals: 'structural changes', here, can only affect either the matrix Z or the distributions of random shocks. It is also useful for constructing counterfactual simulations, since the same structure can be applied to different distributions of education by genders, using standard techniques to solve for the stable equilibrium of the corresponding matching game.¹

2.6 The $n \times n$ case

Extending the previous results to any number of educational categories raises a fundamental problem: one cannot expect assortativeness to be uniform (or to vary uniformly) across the various categories. For instance, matching patterns can be positive assortative at the top of the distribution but not at the bottom (or conversely); and assortativeness may, over a given

¹See Chiappori, Costa-Dias, Crossman and Meghir (2020) and Chiappori, Costa-Dias and Meghir (2020) for an application of these ideas.

period, increase among more educated groups while declining among the less educated ones. In that sense, the ambition of summarizing the *global* evolution of assortativeness by a single index is fraught with dangers, and can actually generate misleading results. A comparison of assortativeness between two $n \times n$ Tables, even using the same index, can be performed in various ways, potentially leading to different conclusions, simply because it is sensitive to the choice of aggregation over several groups (or education levels in our running example). In particular, statements like 'educational homogamy did not change over a given period' should be handled with care, at least when they are based on a single measure: they may reflect the absence of any variation, but also the net outcome of potentially large changes operating in opposite directions for different subsets of the population.

In [Chiappori, Costa-Dias and Meghir \(2020\)](#), we discuss several possible strategies for extending the previous analysis to the $n \times n$ case. One option is to concentrate on one particular education category - say, the most educated - and 'merge' the remaining categories into a single, 'everybody else' class. In this case, variations in assortativeness in different margins would be concealed by the aggregation of many categories into a single one.

3 Empirical example: educational homogamy among educated people in the US

The sensitivity of the likelihood ratio to the mass of people in the group of interest may explain the discrepancies between the results in [Eika et al. \(2019\)](#) and those reported by the rest of the literature. Specifically, that study uses estimates of the likelihood ratio to demonstrate that assortative matching has declined among college graduates over the recent past (page 2085).

While we do not dispute the numbers in that study, we argue that their interpretation in terms of a decline in assortative matching among educated people is incorrect because the likelihood ratio is not a reliable measure of assortativeness. In this particular case,

the conclusion may mostly reflect the significant increase in college education for men and (especially) women over the period.

That increase in education is illustrated in Table 1. The figures in the Table are estimated on the same data from the March extract of the US Current Population Survey that is used in Eika et al. (2019). Here we consider two birth cohorts, 1950-59 and 1970-75. The educational choices of these two cohorts were taken under very different scenarios about the college premium, with the later cohort facing a much higher market return to college education than the earlier one. Consistently with that change, the Table shows that the number of college educated men and women increased between the two cohorts and that the change was especially marked among women, who became more educated than men. Moreover, the increasing concentration of married individuals among college graduates comes entirely at the expense of fewer individuals in the bottom education group.

Table 1: Distribution of education among married men and women – birth cohorts 1950-59 and 1970-75

	High School and below	Some College	4+ years College degree
Birth cohort 1950-59			
Men	43.1	25.6	31.3
Women	46.8	27.2	26.0
Birth cohort 1970-75			
Men	37.0	25.3	37.7
Women	30.7	27.0	42.3

Data source: March extract of the US Current Population Survey, subsample of married individuals observed when aged 35-44 and born in 1950-59 or 1970-75.

Theory predicts that preferences for homogamy should increase as a result of the increase in the college premium (Chiappori et al., 2017). Estimates in Table 2 show how the various indices describe changes in PAM at the top of the education distribution across the two cohorts. They refer to three different 2×2 tables, comparing College graduates with the education group just below (column 1) and with everyone who did not graduate from College (column 2), as well as those who attended College with those who did not (column 3).

Table 2: Marital assortativeness at the top of the distribution of education – comparing birth cohorts 1950-59 and 1970-75

	College vs Some College	College vs less than College	At least Some College vs High School and below
Panel A: Odds ratio			
diff. across cohorts	0.214	0.061	0.293
adjusted p -value	0.000	0.044	0.000
Panel B: χ^2			
diff. across cohorts	0.029	0.040	0.032
adjusted p -value	0.000	0.000	0.000
Panel C: Minimum Distance			
diff. across cohorts	0.001	0.026	0.071
adjusted p -value	0.888	0.000	0.000
Panel D: Likelihood ratio			
diff. across cohorts	-0.046	-0.421	-0.125
adjusted p -value	0.000	0.000	0.000

Notes: Columns identify each of the 2×2 sorting matrices. In each panel, row 1 shows estimates of the difference in the respective index between the latest and earliest cohorts; row 2 shows p -values for 2-sided significance testing adjusted for multiple hypothesis using the stepdown method for the three outcomes on the row. (Romano and Wolf (2005), Romano et al. (2008), Romano and Wolf (2016)). *Data source*: March extract of the US Current Population Survey, subsample of married individuals observed when aged 35-44 and born in 1950-59 or 1970-75.

We see that, in all cases, the odds ratio, the χ^2 and the minimum distance index, which all satisfy Symmetry and Weak Perfect PAM, conclude that assortativeness significantly increased between the two cohorts. On the contrary, the likelihood ratio shows a significant reduction.²

4 Concluding Remarks

It is relatively simple to estimate whether there is positive assortative matching in a stochastic marriage market along the dimensions of a characteristic such as education. However, measuring the extent to which such assortative matching differs between two economies or between two points in time for the same economy is challenging when the marginal distributions of the characteristics also change. Drawing from the statistics literature we define

²It should however be noted that the conclusions may depend on the definition of education classes, as shown by Gihleb and Lang (2016).

simple conditions that any index should satisfy to provide a measure of change in sorting that is not distorted by changes in the marginal distributions of the characteristic. We show that most frequently used indices satisfy these conditions but that the likelihood criterion of Eika et al. (2019) does not. This difference in properties may underlie the contrasting conclusions about the change in homogamy over the recent decades.

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