

**COWLES FOUNDATION FOR RESEARCH IN ECONOMICS  
AT YALE UNIVERSITY**

**Box 2125, Yale Station  
New Haven, Connecticut**

**COWLES FOUNDATION DISCUSSION PAPER NO. 189**

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**INVESTMENT IN HUMANS, TECHNOLOGICAL DIFFUSION AND ECONOMIC GROWTH**

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**August 12, 1965**

# INVESTMENT IN HUMANS, TECHNOLOGICAL DIFFUSION AND ECONOMIC GROWTH

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## I. Introduction

Most economic theorists have embraced the principle that certain kinds of education -- the three R's, vocational training and higher education -- equip a man to perform certain jobs or functions, or enable a man to perform a given function more effectively. The principle seems a sound one. Underlying it, perhaps, is the theory that education enhances one's ability to receive, decode and understand information and that information processing and interpretation is important for performing or learning to perform many jobs.

In applying this principle we find it fruitful to classify jobs or functions according to the degree to which they require adaptation to change or require learning in the performance of the function. At the bottom of this scale are functions which are highly routinized: e.g., running a power saw or diagnosing a malfunction in an automobile. In these functions, the discriminations to be made and the operations based on them remain relatively constant over time. In the other direction on this scale we have, for example, innovative functions which demand keeping

abreast of improving technology. Even a highly routinized job may require considerable education to master the necessary discriminations and skills. But probably education is especially important to those functions requiring adaptation to change. Here it is necessary to learn to follow and to understand new technological developments.

Thus far, economic growth theory has concentrated on the role of education as it relates to the completely routinized job. In its usual, rather general form, the theory postulates a production function which states how maximum current output depends upon the current services of tangible capital goods, the current number of men performing each of these jobs, possibly the current educational attainments of each of these jobholders and possibly time. To simplify matters, some analysts have specified a production function in which output depends upon tangible capital and "effective labor"; the latter is a weighted sum of the number of workers, the weight assigned to each worker being an increasing function of that worker's educational attainment. This specification assumes that highly educated men are perfect substitutes for less educated men (in the technical sense that the marginal rate of substitution between them is constant). Actually, it is possible that educated men are more substitutable for certain capital goods than for other labor; they permit production with less complex machines. However, the exact specification of the production function does not concern us. The pertinent feature of this kind of production function is this: The "marginal productivity" of

education, which is a function of the inputs and the current technology, can remain positive forever even if the technology is stationary. In the models we shall later introduce, education has a positive payoff only if the technology is always improving.

We shall consider now the importance of education for a particular function requiring great adaptation to change. We then propose two models which these considerations suggest.

## II. The Hypothesis

We suggest that, in a technologically progressive or dynamic economy, production management is a function requiring adaptation to change and that the more educated a manager is, the quicker will he be to introduce new techniques of production. To put the hypothesis simply, educated people make good innovators, so that education speeds the process of technological diffusion.

Evidence for this hypothesis can be found in the experience of United States agriculture.<sup>1</sup> It is clear that the farmer with a relatively high level of education has tended to adopt productive innovations earlier than the farmer with relatively little education. We submit that this is because the greater education of the more educated farmer has increased his ability to read and understand the information on new products and processes disseminated by the Department of Agriculture, the farm journals, the radio, seed and equipment companies and so on.<sup>2</sup>

The better educated farmer is quicker to adopt new processes and products since, for him, the expected payoff from innovation is likely to be greater and the risk likely to be smaller. This is because he is better able to discriminate between promising and unpromising ideas, and hence less likely to make mistakes. The less educated farmer, for whom the information in technical journals means less, is prudent to delay the introduction of a new technique until he has concrete evidence of its profitability, like the fact that his more educated friends have adopted the technique with success.

This phenomenon, that education speeds technological diffusion, may take different forms outside of agriculture. In large, industrial corporations, in which there is a fine division of labor, the function of keeping abreast of technological improvements (though perhaps not the ultimate responsibility for innovation) may be assigned to scientists. In this case, their education is obviously important; but so too is the education and sophistication of top management which must make the final decisions.<sup>3</sup>

So much for our broad hypothesis and the evidence supporting it. We shall consider now two specific models of the process of technological diffusion and the role of education.

### III. Two Models of Technological Diffusion

We shall adopt a postulate about the factor-saving character of technical progress which permits us to speak meaningfully about the "level" or "index" of technology. Specifically, we suppose that technical progress is Harrod-neutral everywhere (i.e., for all capital-labor ratios) so that progress can be described as purely labor-augmenting. This means that if output,  $Q$ , is a function of capital,  $K$ , labor,  $L$ , and time,  $t$ , the production function may be written

$$(1) \quad Q(t) = F[K(t), A(t) L(t)]$$

In (1), the variable  $A(t)$  is our index of technology in practice. If we interpret (1) as a vintage production function in which  $K(t)$  is the quantity of currently produced capital,  $L(t)$  the labor working with it and  $Q(t)$  the output producible from it, then  $A(t)$  measures the best-practice level of technology, the (average) technology level "embodied" in the capital goods currently being produced. Alternatively, we could suppose that all technical progress is wholly "disembodied" and that (1) is the "aggregate" production function for the firm, industry or economy and  $A(t)$  is the (average) index of technology common to all vintages of capital, old and new.

In addition to this concept, we introduce the notion of the theoretical level of technology,  $T(t)$ . This is defined as the level of

technology in practice that would exist if technological diffusion were completely instantaneous. It is a measure of the stock of knowledge or body of techniques that is available to innovators. We shall suppose that the theoretical technology level advances exogeneously at a constant exponential rate  $\lambda$  :

$$(2) \quad T(t) = T_0 e^{\lambda t}, \quad \lambda > 0$$

First model. Our first model is as simple a one as we can invent. It states that the time lag between the creation of a new technique and its adoption is a decreasing function of some index of average educational attainment,  $\underline{h}$ , of those in a position to innovate. (We may think of  $\underline{h}$  as denoting the degree of human capital intensity.) Letting  $\underline{w}$  denote the lag, we can represent this notion as follows:

$$(3) \quad A(t) = T(t - w(h)), \quad w'(h) < 0 .$$

The level of technology in practice equals the theoretical level of technology  $\underline{w}$  years ago,  $\underline{w}$  a decreasing function of  $\underline{h}$  .

Substitution of (2) in (3) yields

$$(4) \quad A(t) = T_0 e^{\lambda[t - w(h)]}$$

If  $\underline{h}$  is constant, two results follow from (4). First, the index of technology in practice grows at the same rate,  $\lambda$ , as the index of theoretical technology. Second, the "level" or path of the technology in practice is an increasing function of  $\underline{h}$ , since an increase of  $\underline{h}$  shortens the lag between  $T(t)$  and  $A(t)$ .

An important feature of this model is that (ceteris paribus) the return to education is greater the faster the theoretical level of technology has been advancing. As equation (5) shows, the effect upon  $A(t)$  of a marginal increase of  $\underline{h}$  is an increasing function of  $\lambda$ , given  $A(t)$ , and is positive only if  $\lambda > 0$ .

$$(5) \quad \begin{aligned} \frac{\partial A(t)}{\partial h} &= -\lambda w'(h) T_0 e^{\lambda[t - w(h)]} \\ &= -\lambda w'(h) A(t) . \end{aligned}$$

The same property is displayed by the "marginal productivity of educational attainment". Using (1) and (4) we have

$$(6) \quad Q(t) = F[K(t), T_0 e^{\lambda[t - w(h)]} L(t)]$$

Hence,

$$(7) \quad \begin{aligned} \frac{\partial Q(t)}{\partial h} &= \lambda T_0 e^{\lambda[t - w(h)]} L(t) [-w'(h)] F_2 \\ &= -\lambda w'(h) \times \text{Wage Bill} . \end{aligned}$$



Thus the marginal productivity of education is an increasing function of  $\lambda$ , given the current wage bill, and is positive only if  $\lambda > 0$ . This feature is not found in the conventional treatment of education described at the beginning of this paper.

This first model is not altogether satisfactory. It is unreasonable to suppose that the lag of the best-practice level behind the theoretical level of technology is independent of the profitability of the new techniques not yet introduced. Further, it is somewhat unrealistic to suppose that an increase of educational attainments instantaneously reduces the lag. In these respects, our second model is somewhat more realistic.

Second model. Our second model states that the rate at which the latest, theoretical technology is realized in improved technological practice depends upon educational attainment and upon the gap between the theoretical level of technology and the level of technology in practice. Specifically,

$$(8) \quad \dot{A}(t) = \phi(h) [T(t) - A(t)]$$

or equivalently

$$(8') \quad \frac{\dot{A}(t)}{A(t)} = \phi(h) \left[ \frac{T(t) - A(t)}{A(t)} \right], \quad \phi(0) = 0, \quad \phi'(h) > 0.$$

According to this hypothesis, the rate of increase of the technology in practice (not the level) is an increasing function of education attainment and proportional to the "gap",  $(T(t) - A(t))/A(t)$ .

Some results parallel to those in the first model can be obtained if we again postulate exponential growth of  $T(t)$ , as in (2), and constancy of  $\underline{h}$ . First in the long run, if  $\underline{h}$  is positive, the rate of increase of the level of technology in practice,  $\dot{A}(t)/A(t)$ , settles down to the value  $\lambda$ , independently of the index of education attainment. The reason is this: if, say, the level of  $\underline{h}$  is sufficiently large that  $\dot{A}(t)/A(t) > \lambda$  initially, then the gap narrows; but the narrowing of the gap reduces  $\dot{A}(t)/A(t)$ ; the gap continues to narrow until, in the limit,  $\dot{A}(t)/A(t)$  has fallen to the value  $\lambda$  at which point the system is in equilibrium with a constant gap.

Another result is that the asymptotic or equilibrium gap is a decreasing function of educational attainment. Thus increased educational attainment increases the path of the technology in practice in the long run.

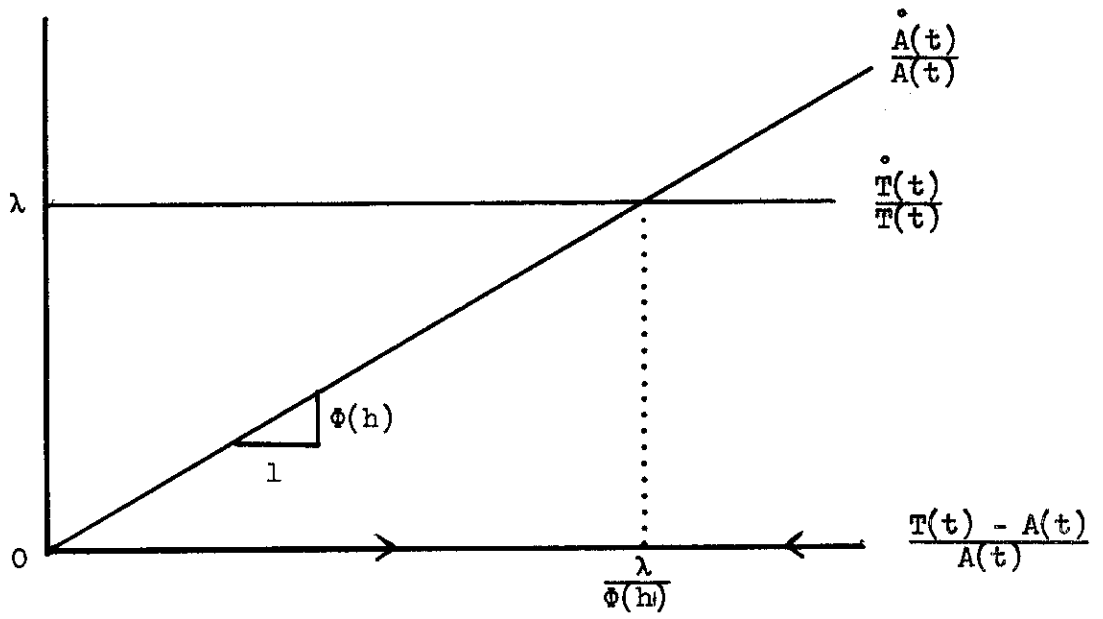
Both these results are shown by Figure 1 and by (9), which is the solution to our differential equation (8), given (2):

$$(9) \quad A(t) = \left( A_0 - \frac{\Phi}{\Phi + \lambda} \right) e^{-\Phi t} + \frac{\Phi}{\Phi + \lambda} T_0 e^{\lambda t} .$$

As both (9) and Figure 1 imply, the equilibrium path of the technology in practice is given by

$$(10) \quad A^*(t) = \frac{\Phi(\underline{h})}{\Phi(\underline{h}) + \lambda} T_0 e^{\lambda t} ;$$

FIGURE 1



the equilibrium gap is given by

$$(11) \quad \frac{T(t) - A^*(t)}{A^*(t)} = \frac{\lambda}{\Phi(h)} \cdot$$

In a technologically stagnant economy ( $\lambda = 0$ ), the gap approaches zero for every  $h > 0$ . In a technologically progressive economy ( $\lambda > 0$ ), there is a positive equilibrium gap for every  $h$  and  $\lambda$ . The equilibrium gap is increasing in  $\lambda$  and decreasing in  $h$ .

In the first model it was seen that the marginal productivity of educational attainment is an increasing function of  $\lambda$  and positive only if  $\lambda > 0$ . That is also true of the second model in the long run (once the effect of an increase of  $h$  has had time to influence the level of  $A(t)$  as well as its rate of change). Equation (12) shows that the elasticity of the long-run equilibrium level of technology in practice,  $A^*(t)$ , with respect to  $h$  is increasing in  $\lambda$ :

$$(12) \quad \frac{\partial A^*(t)}{\partial h} \frac{h}{A^*(t)} = \left[ \frac{h\Phi'(h)}{\Phi(h)} \right] \left[ \frac{\lambda}{\Phi(h) + \lambda} \right]$$

This indicates that the payoff to increased educational attainment is greater the more technologically progressive is the economy.

These are only partial models and excessively simple ones. No machinery has been given for determining educational attainment.<sup>4</sup>

The theoretical level of technology has been treated as exogenous. Finally, it might be useful to build a model which combines elements of both the first and second model: the rate of technical progress in practice may depend both upon the length of time during which a new technique has been in existence and upon its profitability. But we hope that these two models may be a useful starting point.

#### IV. Concluding Remarks

The general subject at this session is the relationships between capital structure and technological progress. Recalling that the process of education can be viewed as an act of investment in people, that educated people are bearers of human capital, we see that this paper has relevance to that subject. For, according to the models presented here, the rate of return to education is greater the more technologically progressive is the economy. This suggests that the progressiveness of the technology has implications for the optimal capital structure in the broad sense. In particular, it may be that society should build more human capital relative to tangible capital the more dynamic is the technology.

Another point of relevance for social investment policy may be mentioned. If innovations produce externalities, because they show the way to imitators, then education -- by its stimulation of innovation -- also yields externalities. Hence, the way of viewing the role of education in economic growth set forth here seems to indicate another possible source of a divergence between the private and social rate of return to education.

FOOTNOTES

1. See E. M. Rogers, Diffusion of Innovations (Glencoe, Ill.: The Free Press, 1962), especially Chapter 6.
2. To be sure, some of the correlation described between education and diffusion may be spurious: Some farmers are undoubtedly both progressive and educated because they come from progressive and prosperous farming families that could afford to give them an education. But there is no question that educated farmers do read technical, innovation-describing literature more than do less educated farmers -- and presumably because they find it profitable to do so.
3. For an interesting essay on science policy, in which it is argued that Britain's growth has suffered from a shortage of scientists in management, that too small a fraction of scientists are engaged in using (rather than adding to) the existing stock of knowledge, see C. F. Carter and B. R. Williams, "Government Scientific Policy and the Growth of the British Economy", The Manchester School, Vol. 32 (September, 1964).
4. This is done in a paper by Phelps which develops a Golden Rule of Education. It is shown that Golden Rule growth requires more education the more technologically progressive is the economy.