

# Ambiguity Aversion, Malevolent Nature, and the Variational Representation of Preferences\*

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## Abstract

In the classic Anscombe and Aumann decision setting, we give necessary and sufficient conditions that guarantee the existence of a *utility function*  $u$  on outcomes and an *ambiguity index*  $c$  on the set of all probabilities on the states of the world such that, for all acts  $f$  and  $g$ ,

$$f \succsim g \Leftrightarrow \min_p \left( \int u(f) dp + c(p) \right) \geq \min_p \left( \int u(g) dp + c(p) \right).$$

The function  $u$  represents the decision maker's risk attitudes, while the index  $c$  captures his ambiguity attitudes.

The preferences we characterize include as special cases the *multiple priors preferences* of Gilboa and Schmeidler, the *multiplier preferences* of Hansen and Sargent, and the *mean-variance preferences* of Markowitz and Tobin. In this way we are able to provide a rigorous decision-theoretic foundation on the latter two models, which have been widely used in macroeconomics and finance.

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